# Crystal and molecular structures of diazapyrenes and a study of $\pi \cdots \pi$ interactions $\dagger$ 

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#### Abstract

Two diazapyrenes, 5,10-dimethyl-4,9-diazapyrene (1) and novel 2,7-dimethyl-4,9-diazapyrene (2) have been synthesized. Their crystal structures are reported here and are the first representatives of diazapyrenes. Crystal data: (1) monoclinic, $P 2_{1} / c, a=4.0246$ (5), $b=$ 15.5147 (5), $c=9.1453$ (9) A, $\beta=101.23(1)^{\circ}, V=$ 560.1 (1) $\AA^{3}, Z=2, R=0.043$; (2) monoclinic, $C 2 / m, a=$ 12.4968 (3), $b=11.4751$ (4), $c=3.9615$ (5) Å, $\beta=$ $96.80(1)^{\circ}, V=564.09(5) \AA^{3}, Z=2, R=0.0405$. The experimental bond lengths are compared with those calculated by molecular mechanics (MM3), semiempirical methods (MOPAC6.0-PM3, AM1, MNDO) and values predicted by valence-bond and variableelectronegativity self-consistent field (VESCF) methods. $\pi \cdots \pi$ interactions in (1), (2) and seventeen other pyrene and pyrene-like molecules selected from the Cambridge Structural Database [Allen \& Kennard (1993). Chem. Des. Autom. News, 8, 131-137] have been studied. The following quantitative parameters of $\pi \cdots \pi$ interactions have been calculated: the shortest crystallographic axis, the offset parameter, the interplanar angle, the interactive volume and the overlapping surfaces. They are used for the classification of crystal-packing motifs; a high predominance of $\beta$ and a few cases of $\gamma$ and sandwich-herringbone types are observed. In addition, electronegativity, the sum of partial atomic charges of the ring non- H atoms and the number of aromatic skeleton electrons are used as parameters for classification. MOPAC-PM3 was used to calculate the partial atomic charges in (1), (2) and pyrene analogues. Correlations between geometrical and electronic structure parameters reveal an analogy between the $\beta$-type structures and the crystal structure of graphite.


## 1. Introduction

Non-covalent interactions between delocalized $\pi$ systems of aromatic molecules play a considerable role in molecular recognition and molecular aggregation. $\pi \cdots \pi$ interactions (Hunter, 1994; Hunter \& Sanders, 1990) are of interest in structural molecular biology,

[^0]materials science and host-guest chemistry (D'Souza \& Maitra, 1996), and supramolecular chemistry (Webb \& Wilcox, 1993). One of the most intriguing phenomena in biology involving $\pi \cdots \pi$ interactions is the intercalation of neutral or charged aromatic compounds between adjacent base pairs of double-stranded DNA (Wilson, 1989; Wakelin, 1986). Various natural (Bailly et al., 1990) or synthetic (Denny et al., 1983; Wilson et al., 1988) intercalators are known. However, numerous problems remain, including the design of a reliable model to predict the strength of the interaction and the preferred intercalation site (Veal et al., 1990; Sponer \& Hobza, 1996; Sponer et al., 1996).

The 4,9-diazapyrenes are described here to see how they can be used as DNA intercalators or as DNA base analogues. As there are no structural data available for this class of aromatic system, they are compared with analogous pyrene and pyrene-like molecules.

Among the most efficient and the most thoroughly studied intercalators is the phenanthridine derivative ethidium cation, with a formal positive charge on the phenanthridine N atom [(3) in Fig. 1] (Sobell et al., 1977; Meyer-Almes \& Porschke, 1993; Sarfati et al., 1995). Recently, Lehn and coworkers (Blacker et al., 1987) and Brunn \& Harriman (1991) described the DNA-intercalation properties of the 2,7-diazapyrenium system. It turned out that this dication is efficient in the cleaving of DNA in visible light (Blacker et al., 1986). These results focused our attention on the isomeric 4,9-diazapyrenium system. Surprisingly, very little is known about the

(1)

(2)

(3)

Fig. 1. Chemical diagrams for 5,10-dimethyl-4,9-diazapyrene, (1), 2,7-dimethyl-4,9-diazapyrene, (2), and ethidium, (3).


PYRENE02 pyrene


NAPSEZ10
naphto[1,8-cd:4,5-c' $\left.d^{\prime}\right]$ bis $[1,2$, sselenadiazine


2
2,7-dimethyl-
4,9-diazapyrene

vOXLOJ 1,6-dioxapyrene


DMPYRN 2,7-dimethylpyrene


KENDEM
1,4,5,8-naphthalenetetracarboxylic dianhydride


DOXTEP 1,6-dithiapyrene


NAPTDZ10
naphto[1,8-cd:4,5-c' $\left.d^{\prime}\right]$ bis $[1,2,6]$ thiadiazine


BUTPYR10
2,7-di- $t$-butylpyrene



1
5,10-dimethyl-
4,9-diazapyrene


Chem. Phys. Lett. 258,1996,490 perdeuteropyrene


1-pyrenebutanoic acid


ZEDDIV01
$N$-(2-hydroxy-1-naphthylmethylene)-1-pyreneamine


TFHCPY 10
1,3,6,8-tetrafluoro-2,4,5,7,9,10hexachloropyrene


KASZAF01
$N, N$-disalicylidene-1,6-pyrenediamine

Fig. 2. Chemical diagrams for the compounds used for the analysis with CSD REFCODEs and chemical names.
chemistry, and almost nothing about the biological properties, of 4,9-diazapyrene and its cations; the synthesis of a few representatives was described forty years ago (Fairfull et al., 1952; Badger \& Sasse, 1957; Mosby, 1957).

4,9-Diazapyrenes and their derivatives have been studied as part of research related to the synthesis, chemical characterization and biological properties of novel DNA intercalators and potential DNA base analogues (Piantanida, 1997). Some of the 4,9-diazapyrenium compounds were recognized to be very potent in inducing apoptosis in human tumour cells, whereas this effect was small on normal cells (Steiner-Biočić et al., 1996). These interesting biological properties and the fact that they were studied very little in the past justify our work.

The crystal packing, based on stacked layers, is analysed as a model for $\pi \cdots \pi$ interactions effective in intercalation using the crystal structures of 5,10-dime-thyl-4,9-diazapyrene, (1), its 2,7-dimethyl analogue, (2), (Fig. 1) and seventeen pyrene derivatives and pyrenelike systems (Fig. 2) extracted from the Cambridge Structural Database (CSD; Allen \& Kennard, 1993). The crystal structures were classified according to the approach given by Desiraju and Gavezzotti (Gavezzotti \& Desiraju, 1988; Desiraju \& Gavezzotti, 1989) indicating $\pi \cdots \pi$ interactions between neighbouring molecules. The quantitative analysis of this interaction was based on the offset parameter, the interplanar angle, overlapping surfaces (stacking areas), the interactive volume and the shortest crystallographic axis (Fig. 3), as well as the average atomic electronegativity after Pauling (Shriver et al., 1990), the number of delocalized, localized and free electrons, and the sum of the partial atomic charges of the non- H ring atoms of the sixteen pyrene skeleton atoms [obtained using MOPAC-PM3 (Stewart, 1990a,b; MOPAC, 1990)].

The interaction energy between adjacent molecules in the crystal was evaluated using the empirical potential given by Gavezzotti (1994) and the program PLUTO (Motherwell, 1997) implemented in the CSD. The relationships between bond lengths and bond orders for C C and $\mathrm{C}-\mathrm{N}$ bonds of diaza- and polyazabenzenoids, computed by valence-bond and molecular-orbital methods, were found using linear-regression analysis. The molecular structures of (1) and (2) were reproduced by molecular mechanics and semi-empirical methods and were compared with experimental data.

## 2. Experimental

### 2.1. Preparation of (1) and (2)

5,10-Dimethyl-4,9-diazapyrene, (1), previously described by Mosby (1957) and novel 2,7-dimethyl-4,9diazapyrene, (2), were prepared by the modified Mosby
procedure (1957). 2,2'-Diacetamidobiphenyl or $2,2^{\prime}$ -diformamido-4,4'-dimethylbiphenyl (Piantanida, 1997) ( 3 mmol ) was mixed with anhydrous $\mathrm{AlCl}_{3}(113 \mathrm{mmol})$ and $\mathrm{NaCl}(60 \mathrm{mmol})$, and heated to melt at $523-543 \mathrm{~K}$. The melt was heated for 2 h at this temperature under vigorous stirring. After cooling to 423 K , the melt was poured onto ice ( 100 g ) and made alkaline ( pH 10 ) with $5 \mathrm{~mol} \mathrm{dm}{ }^{-3} \mathrm{NaOH}$. The precipitate was collected, dried and subjected to continuous extraction with $\mathrm{CHCl}_{3}$ for 20 h . The solvent was evaporated and the solid residue purified by column chromatography on silica gel using $5 \% \mathrm{MeOH}$ in $\mathrm{CH}_{2} \mathrm{Cl}_{2}$ as eluant. Recrystallizations from $\mathrm{CHCl}_{3}$ gave (1) and (2) in 15 and $20 \%$ yield, respectively. Data for (1): ${ }^{1} \mathrm{H}$ NMR ( $300 \mathrm{MHz}, \mathrm{CDCl}_{3}$ ): 3.19 $(6 \mathrm{H}, s), 8.17(2 \mathrm{H}, t), 8.40(2 \mathrm{H}, d), 8.51(2 \mathrm{H}, d)$. Data for (2): m.p. 523-525 K; IR (KBr): 3000, 1570, 1460, 1410, 1305, 1268, $930 \mathrm{~cm}^{-1}$; ${ }^{1} \mathrm{H}$ NMR ( $300 \mathrm{MHz}, \mathrm{CDCl}_{3}$ ): 2.89 $(6 \mathrm{H}, s), 8.22(2 \mathrm{H}, s), 8.49(2 \mathrm{H}, s), 9.64(2 \mathrm{H}, s)$; HRMS (FAB): calculated for $\mathrm{C}_{16} \mathrm{H}_{12} \mathrm{~N}_{2}\left(M^{+}\right)$232.100, found 232.099; analysis of $\mathrm{C}_{16} \mathrm{H}_{12} \mathrm{~N}_{2}$ : calculated C 82.73, H 5.21, N 12.06; found C 82.89 , H 5.33, N $12.23 \%$.

(a)


(b)

(e)

$\mathrm{P}_{1}=\mathrm{A} \cap \mathrm{B}$
$\mathrm{P}_{2}=\mathrm{B} \cap \mathrm{C}$
(g)

(c)

(f)

$\mathrm{S}_{3}=\mathrm{P}_{1} \cap \mathrm{P}_{2}$

Fig. 3. Geometrical parameters used for the definition and classification of packing types of pyrenes and analogues: $(a)$ 'centre-tocentre' offset $v(\AA),(b)$ interplanar distance $d(\AA)$, the shortest axis $p(\AA)$ and the angle $\varphi\left({ }^{\circ}\right) ;(c)$ interplanar angle $\theta\left({ }^{\circ}\right)$ between adjacent stacks, interactive volume $V=2 S_{2} d\left(\AA^{3}\right)$ which defines a space between the reference molecule and its two closest neighbours in the stack; overlapping surfaces of the reference molecule viewed perpendicular to the least-squares planes of the aromatic rings with $(d)$ a single neighbour, $S_{1}\left(\AA_{\circ}^{2}\right)$, (e) two neighbours, $S_{2}\left(\AA^{2}\right)$ and $(f)$ three neighbours, $S_{3}\left(\AA^{2}\right) ;(g)$ the overlapping surfaces were calculated as the areas of intersecting polygons with their definition using set theory; the reference molecule is represented as the set B and intersections $S_{1}, S_{2}$, and $S_{3}$ of the three sets are equivalent to $S_{1}, S_{2}$, and $S_{3}$.

### 2.2. Electronic absorption and fluorescence emission spectra of (1) and (2)

The electronic absorption spectra of the isomeric dimethyl-4,9-diazapyrene derivatives (1) and (2) recorded in EtOH at concentrations of $1.86 \times 10^{-5}$ and $1.84 \times 10^{-5} \mathrm{~mol} \mathrm{dm}^{-3}$, respectively, are shown in Fig. 4. The following absorptions ( $\lambda_{\text {max }}, \mathrm{nm} ; \varepsilon_{\max }$ ) are observed: (1): 243.1 (49408), 257.9 (16451), 268.7 (16505), 321.9 (12258), 336.7 (14667), 364.7 (3871), 376.0 (2849), 384.1 (7634); (2): 238.5 (48967), 258.9 (20760), 269.1 (30652), 317.1 (13260), 330.9 (15054), 351.9 (5706), 370.5 (10380). The spectra of (1) and (2) are similar. However, a bathochromic shift on going from (1) to (2) was observed, particularly in the $300-400 \mathrm{~nm}$ region. The spectra of both (1) and (2) exhibit enhanced hypochromic effects with increasing concentration. The concentration-absorption behaviour at selected wavelengths shows clear deviation from linearity above concentrations of $1 \times 10^{-4} \mathrm{~mol} \mathrm{dm}^{-3}$ for (1) and above $2 \times 10^{-4} \mathrm{~mol} \mathrm{dm}^{-3}$ for (2). These effects point to the


Fig. 4. UV/VIS spectra (EtOH) of compounds (1) (dashed line) and (2) (solid line) $c=1.86 \times 10^{-5}$ and $1.84 \times 10^{-5} \mathrm{~mol} \mathrm{dm}^{-3}$, respectively.


Fig. 5. Fluorescence spectra (EtOH) of compounds (1) (dashed line, $c=$ $7.19 \times 10^{-6} \mathrm{~mol} \mathrm{dm}^{-3}$ ) and (2) (solid line, $c=9.18 \times$ $10^{-6} \mathrm{~mol} \mathrm{dm}^{-3}$ ).
strong tendency of both (1) and (2) to form stacked aggregates in solution.
The fluorescence emission spectra of (1) $(c=7.19 \times$ $10^{-6} \mathrm{~mol} \mathrm{dm}^{-3}$ ) and (2) $\left(c=9.18 \times 10^{-6} \mathrm{~mol} \mathrm{dm}^{-3}\right)$ dissolved in ethanol are shown in Fig. 5 and confirm the effect of the substitution pattern on the electronic absorption and fluorescence properties of the 4,9diazapyrene system.

### 2.3. Crystal structure determinations of (1) and (2)

Crystal data, including data collection parameters and details of the structure refinements, are listed in Table 1. Light-sensitive crystals of (1) were grown in the dark at room temperature from a mixture of dichloromethane and dimethyl sulfoxide. Dichloromethane was used for the crystallization of (2). Data were collected at room temperature and, for (1), in the dark. Data collection and cell refinement were carried out using $C A D-4$ EXPRESS (Enraf-Nonius, 1992). Data reduction was performed with the program HELENA (Spek, 1990b). The structures were solved by direct methods (SHELXS86) (Sheldrick, 1990) and refined with SHELXL93 (Sheldrick, 1993) on $F^{2}$. Scattering factors were from SHELXL93. The H-atom coordinates of both compounds were determined from difference Fourier maps with the exception of those of the methyl groups in (2), which were calculated on stereochemical grounds. All H -atom positions were refined. The molecules (1) and (2) have a crystallographic inversion centre in the middle of the C11-C11a bond (Figs. 6 and 7). The crystallographic symmetry of molecule (2) is $C_{2 h}$. In


Fig. 6. Molecular structure of (1) [ORTEPII (Johnson, 1976), 30\% probability level ellipsoids] with the atom numbering (according to Chemical Abstracts); symmetry code: (a) $-x, 1-y,-z$.

Table 1. Experimental details

Crystal data
Chemical formula
Cell setting
Space group
$a(\AA$ )
$b(\AA$ © $)$
$c(\AA)$
$\beta\left({ }^{\circ}\right)$
$V\left(\AA^{3}\right)$
Z
$D_{x}\left(\mathrm{Mg} \mathrm{m}^{-3}\right)$
Radiation type
Wavelength ( $\AA$ )
No. of reflections for cell para-
meters
$\theta$ range ( ${ }^{\circ}$ )
$\mu\left(\mathrm{mm}^{-1}\right)$
$F_{000}$
Temperature (K)
Crystal form
Crystal size (mm)
Crystal colour

Data collection
Diffractometer
Data collection method
Absorption correction
No. of measured reflections
No. of independent reflections
No. of observed reflections
Criterion for observed reflections
$R_{\text {int }}$
$\theta_{\text {max }}\left({ }^{\circ}\right)$
Range of $h, k, l$

No. of standard reflections
Frequency of standard reflections
Refinement
Refinement on $F^{2} \quad F^{2}$
$R\left[F^{2}>2 \sigma\left(F^{2}\right)\right]$
$w R\left(F^{2}\right)$
$S$
No. of reflections used in refinement
No. of parameters used
H -atom treatment
Weighting scheme
$(\Delta / \sigma)_{\max }$
$\Delta \rho_{\text {max }}\left(\mathrm{e} \AA^{-3}\right)$
$\Delta \rho_{\text {min }}\left(\mathrm{e} \AA^{-3}\right)$
Extinction method
(1)
$\mathrm{C}_{16} \mathrm{H}_{12} \mathrm{~N}_{2}$
232.286

Monoclinic
$P 2_{1} / c$
4.0246 (5)
15.5147 (5)
9.1453 (9)
101.23 (1)
560.1 (1)

2
1.377
$\mathrm{Cu} K \alpha$
1.54184

18
11-42
0.6

244
295 (3)
Needle
$0.3 \times 0.04 \times 0.04$
Colourless
Enraf-Nonius CAD-4
$\omega / 2 \theta$ scans
None
1297
1135
425
$I>2 \sigma(I)$
0.0360
74.19
$-5 \rightarrow h \rightarrow 0$
$-19 \rightarrow k \rightarrow 0$
$-11 \rightarrow l \rightarrow 11$
3
Every 41 reflections
$F^{2} \quad F^{2}$
0.0425 0.0405
$0.1281 \quad 0.1237$
$0.660 \quad 1.055$
660 508
106
All H -atom parameters refined
$w=1 /\left[\sigma^{2}\left(F_{o}{ }^{2}\right)+(0.1673 P)^{2}\right.$
$+0.5865 P]$ where $P=\left(F_{o}{ }^{2}\right.$
$\left.+2 F_{c}{ }^{2}\right) / 3$
$-0.031$
0.138
$-0.147$
None
(2)

$$
\begin{aligned}
& \mathrm{C}_{16} \mathrm{H}_{12} \mathrm{~N}_{2} \\
& 232.286 \\
& \text { Monoclinic } \\
& C 2 / m \\
& 12.4968(3) \\
& 11.4751(4) \\
& 3.9615(3) \\
& 96.80(1) \\
& 564.09(5) \\
& 2 \\
& 1.369 \\
& \mathrm{Cu} \mathrm{~K} \mathrm{\alpha} \\
& 1.54184 \\
& 21 \\
& \\
& 10.54-42.56 \\
& 0.6 \\
& 244 \\
& 295(2) \\
& \text { Prism } \\
& 0.32 \times 0.14 \times 0.11 \\
& \text { Colourless }
\end{aligned}
$$

Enraf-Nonius CAD-4
$\omega / 2 \theta$ scans
None
1108
508
322
$I>2 \sigma(I)$
0.0425
65.21
$0 \rightarrow h \rightarrow 4$
$-9 \rightarrow k \rightarrow 9$
$-9 \rightarrow l \rightarrow 9$
3
Every 44 reflections
$F^{2}$
0.0405
0.1237

70
All H -atom parameters refined
$w=1 /\left[\sigma^{2}\left(F_{o}{ }^{2}\right)+(0.0966 P)^{2}\right.$
$+0.0939 P]$ where $P=\left(F_{o}{ }^{2}\right.$
$\left.+2 F_{c}{ }^{2}\right) / 3$
0.005
0.19
$-0.12$
None
order to satisfy the symmetry, positional disorder of the atoms N 4 and C4 (Fig. 7) with $50 \%$ population at each site occurred.
The molecular geometry was calculated using the program package PLATON93 (Spek, 1990a). Drawings were prepared using PLUTON (Spek, 1991) and ORTEPII (Johnson, 1976). Final atomic coordinates and
equivalent isotropic displacement parameters are listed in Table 2 for (1) and Table 3 for (2). $\dagger$ Calculations were performed on the Silicon Graphics INDIGO2 work-

[^1]Table 2. Fractional atomic coordinates and equivalent isotropic displacement parameters $\left(\AA^{2}\right)$ for (1)

| $U_{\text {eq }}=(1 / 3) \Sigma_{i} \Sigma_{j} U^{i j} a^{i} a^{i} \mathbf{a}_{i} \cdot \mathbf{a}_{j}$ |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | $x$ | $y$ | $z$ | $U_{\text {eq }}$ |
| N4 | $0.1676(8)$ | $0.35583(19)$ | $0.1291(3)$ | $0.0470(11)$ |
| C1 | $0.4509(10)$ | $0.6138(3)$ | $0.2271(4)$ | $0.0500(17)$ |
| C2 | $0.5860(11)$ | $0.5469(3)$ | $0.3198(4)$ | $0.0536(16)$ |
| C3 | $0.4908(11)$ | $0.4623(3)$ | $0.2872(4)$ | $0.0530(17)$ |
| C5 | $-0.0548(10)$ | $0.3387(2)$ | $0.0075(4)$ | $0.0454(14)$ |
| C11 | $0.1207(9)$ | $0.5102(3)$ | $0.0649(3)$ | $0.0395(12)$ |
| C31 | $0.2587(10)$ | $0.4415(3)$ | $0.1597(4)$ | $0.0444(12)$ |
| C51 | $-0.2135(10)$ | $0.4036(2)$ | $-0.0975(4)$ | $0.043(12)$ |
| C53 | $-0.1415(15)$ | $0.2452(3)$ | $-0.0233(6)$ | $0.062(2)$ |

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### 2.4. Computational methods

For the investigation of the bond length-bond order relationships of $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{N}$ bonds in aza-, diazaand polyazabenzenoids, only the crystal structures of (1) and (2) (this work) are available. Thus, the crystal structures of analogous molecules such as polyazabenzenoids, pyrenes and pyrene-like systems (Fig. 2), and also molecular complexes of pyrene with other aromatic systems, with $R \leq 0.07$ were extracted from the CSD (Allen \& Kennard, 1993). Only the best quality data free from error and disorder, without charged species, solvents, clathrates, metal complexes or organometallic compounds were chosen. For the substituted pyrene-like molecules, only terminal groups attached by single bonds were used. As a single example of a nonplanar molecule, the structure of decachloropyrene (Hazell \& Jagner, 1976) was considered. Data extracted from the CSD were also used for the crystal-packing classification.

Table 3. Fractional atomic coordinates and equivalent isotropic displacement parameters ( $\AA^{2}$ ) for (2)

| $U_{\mathrm{eq}}=(1 / 3) \Sigma_{i} \Sigma_{j} U^{i j} a^{i} a^{j} \mathbf{a}_{i} \cdot \mathbf{a}_{j}$ |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | $x$ | $y$ | $z$ | $U_{\mathrm{eq}}$ |
| N 4 | $0.0454(9)$ | $0.2129(8)$ | $0.940(3)$ | $0.067(5)$ |
| C 1 | $0.20167(13)$ | $0.10471(15)$ | $0.7671(4)$ | $0.0577(6)$ |
| C 2 | $0.25315(17)$ | 0 | $0.7111(6)$ | $0.0574(8)$ |
| C 4 | $0.0510(9)$ | $0.2091(11)$ | $0.953(4)$ | $0.064(5)$ |
| C 11 | $0.05070(15)$ | 0 | $0.9407(5)$ | $0.0456(7)$ |
| C 21 | $0.3642(2)$ | 0 | $0.5974(9)$ | $0.0764(11)$ |
| C 51 | $0.10093(12)$ | $0.10675(14)$ | $0.8818(4)$ | $0.0512(6)$ |

$\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{N} \pi$-bond orders (Kiralj et al., 1996, 1998) for azabenzenoids (Table 4) were calculated by the variable-electronegativity self-consistent field (VESCF) procedure (Allinger et al., 1967) for aromatic systems included in MM3(92) (Allinger, 1992). The molecular geometries of (1) and (2) were reproduced by molecular mechanics using $M M 3$ (92) and by semiempirical methods using MOPAC6.0 (Stewart, 1990a,b; MOPAC, 1990) with PM3 (Stewart, 1989a,b; Dewar et al., 1990; Stewart, 1990a,b), AM1 (Dewar et al., 1985) and MNDO (Dewar \& Thiel, 1977) Hamiltonians and PRECISE and EF keywords (Table 5). PM3 was used to determine partial atomic charges for (1), (2) (Fig. 1), and all the pyrene-like molecules (Fig. 2). The advantage of $P M 3$ over MNDO and AM1 is that, apparently, (i) it reproduces bond lengths and heats of formation reliably, as we found for phenanthrene (Kiralj et al., 1996), diazapyrenes (1) and (2) and pyrene-like molecules, and (ii) partial atomic charges of the pyrene skeleton calculated by PM3 are in between $M N D O$ and $A M 1$ values and can serve for comparison. Regression equations were established and used to evaluate relationships between the bond lengths and the bond orders of diazaand polyazabenzenoids, and to correlate the molecular and crystal-packing properties of (1), (2) and pyrenelike systems (Table 6) using CricketGraph (Stat Works, 1988).


Fig. 7. Molecular structure of (2) [ORTEPII (Johnson, 1976), 30\% probability level ellipsoids] with the atom numbering (according to Chemical Abstracts) and C4, N4 disordered atoms (population parameter $=0.5$ for each atom); symmetry codes: $(a)-x, y, 2-z$; (b) $-x,-y, 2-z ;(c) x,-y, z$.

Table 4. The results of linear-regression analysis of bond length-bond order relationships for $C-C$ and $C-N$ bonds in aza-, diaza- and polyazabenzenoids


Crystal-packing parameters for pyrene-like systems were calculated using the programs PLATON (Spek, 1990a) and PLUTON (Spek, 1991).

The crystal-packing interactions between the pairs of aromatic molecules in the crystals of pyrene, molecular complexes of pyrene with small aromatic systems and pyrene-like systems from the CSD including (1) and (2) were analysed using PLUTO (Motherwell, 1997).

## 3. Results and discussion

3.1. Molecular structures of two diazapyrenes and bond length-bond order relationships for aza-, diaza and polyazabenzenoids

The molecular structures of (1) (Fig. 6) and (2) (Fig. 7) determined by X-ray structure analysis were also evaluated by theoretical methods. To predict the bond lengths in aromatic systems correctly, the bond orders were determined. The results of linear-regression analysis on bond lengths $(d)$ and bond orders $(p)$ for aza-, diaza- and polyazabenzenoids are summarized in Table 4. The largest error ( $0.030 \AA$, Table 4) was detected in polyazabenzenoids for the $\mathrm{C}-\mathrm{N}$ bond calculated by the VESCF approach. In general, both methods, valence-bond and molecular-orbital (using VESCF for aromatic systems), are suitable for
predicting bond lengths in aromatic systems with nitrogen as a heteroatom (Kiralj et al., 1996, 1998).
$\mathrm{C}-\mathrm{C}$ bond lengths in the diazapyrenes (1) and (2) and in pyrene (Hazell et al., 1972) are comparable. Experimental $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{N}$ bond lengths of (1) and (2) are compared with the values calculated by molecular mechanics (MM3) and semi-empirical methods ( $P M 3, A M 1$ and $M N D O$ ) in Table 5. The comparison also includes predicted values obtained from regression analysis ( $d$ versus $p$ ) based on valence-bond (VB) (Herndon, 1974; Herndon \& Párkányi, 1976) and VESCF [Kiralj et al. (1998); procedure for the conjugated system incorporated in MM3(92)] approaches. For molecules (1) and (2) (Table 5) the bond lengths calculated by both methods are comparable with the experimental values and optimized geometries from molecular mechanics and semi-empirical methods. Generally, good agreement between the experimentally determined values and the calculated values is observed; differences are mainly within three standard deviations of the experimentally determined parameters, with the exception of the $\mathrm{C} 2-\mathrm{C} 21$ bond of (2) in PM3 and AM1. For the $\mathrm{C}_{\mathrm{Ar}}-\mathrm{Me}$ single bonds $\mathrm{C} 5-\mathrm{C} 53$ in (1) and $\mathrm{C} 2-$ C21 in (2), the Pauling potential equation (Pauling, 1980) is used. It reproduces bond lengths for zero bond order much better than the regression equations (Kiralj et al., 1998). The predicted values of bond lengths match the experimental values (Table 5).

Table 5. Bond lengths ( $\AA$ ) of (1) and (2) obtained by X-ray structure analysis, molecular mechanics, semi-empirical methods and from regression analysis

|  | $(1)$ | $(2)$ | $(1)$ | $(2)$ | $(1)$ | $(2)$ | $(1)$ | $(2)$ | $(1)$ | $(2)$ | $(1),(2)$ | $(1)$ | $(2)$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | X-ray | X-ray | $M M 3$ | $M M 3$ | $P M 3$ | $P M 3$ | $A M 1$ | $A M 1$ | $M N D O$ | $M N D O$ | VB $\dagger$ | VESCF $\ddagger$ | VESCF $\ddagger$ |
| C1-C2 | $1.383(6)$ | $1.393(2)$ | 1.398 | 1.404 | 1.399 | 1.398 | 1.395 | 1.401 | 1.408 | 1.418 | 1.387 | 1.385 | 1.385 |
| C2-C3 | $1.383(7)$ | - | 1.398 | 1.404 | 1.392 | 1.398 | 1.392 | 1.399 | 1.404 | 1.414 | 1.387 | 1.386 | 1.386 |
| C3-C31 | $1.383(5)$ | - | 1.399 | 1.400 | 1.400 | 1.398 | 1.412 | 1.409 | 1.417 | 1.416 | 1.387 | 1.391 | 1.391 |
| C31-N4 | $1.393(5)$ | - | 1.402 | 1.405 | 1.412 | 1.412 | 1.398 | 1.404 | 1.399 | 1.405 | 1.413 | 1.389 | 1.389 |
| C51-N4 | - | $1.434(10)$ | 1.402 | 1.405 | 1.412 | 1.412 | 1.398 | 1.404 | 1.399 | 1.405 | 1.413 | 1.389 | 1.389 |
| N4-C5 | $1.312(5)$ | - | 1.306 | 1.304 | 1.317 | 1.308 | 1.314 | 1.305 | 1.317 | 1.312 | 1.291 | 1.299 | 1.298 |
| N4-C4a | - | $1.324(16)$ | 1.306 | 1.304 | 1.317 | 1.308 | 1.314 | 1.305 | 1.317 | 1.312 | 1.291 | 1.299 | 1.298 |
| C5-C51 | $1.451(5)$ | - | 1.457 | 1.451 | 1.459 | 1.452 | 1.466 | 1.457 | 1.477 | 1.467 | 1.434 | 1.443 | 1.439 |
| C4-C51 | - | $1.375(13)$ | 1.457 | 1.451 | 1.459 | 1.452 | 1.466 | 1.457 | 1.477 | 1.467 | 1.434 | 1.443 | 1.439 |
| C31-C11 | $1.417(6)$ | - | 1.410 | 1.410 | 1.411 | 1.411 | 1.426 | 1.425 | 1.429 | 1.427 | 1.410 | 1.404 | 1.405 |
| C1-C51a | $1.396(5)$ | - | 1.406 | 1.402 | 1.396 | 1.394 | 1.397 | 1.394 | 1.413 | 1.409 | 1.387 | 1.392 | 1.395 |
| C1-C51 | - | $1.388(2)$ | 1.399 | 1.400 | 1.400 | 1.398 | 1.412 | 1.409 | 1.417 | 1.416 | 1.387 | 1.391 | 1.391 |
| C11-C51a | $1.405(6)$ | - | 1.409 | 1.406 | 1.410 | 1.408 | 1.414 | 1.413 | 1.432 | 1.428 | 1.410 | 1.402 | 1.404 |
| C11-C51 | - | $1.408(2)$ | 1.409 | 1.406 | 1.410 | 1.408 | 1.414 | 1.413 | 1.432 | 1.428 | 1.410 | 1.402 | 1.404 |
| C11-C11a | $1.416(4)$ | $1.403(3)$ | 1.423 | 1.424 | 1.429 | 1.429 | 1.430 | 1.430 | 1.429 | 1.453 | 1.410 | 1.429 | 1.428 |
| C2-CC1 | - | $1.509(3)$ | - | 1.508 | - | 1.487 | - | 1.483 | - | 1.507 | 1.504 | - | 1.497 |
| C5-C53 | $1.506(6)$ | - | 1.511 | - | 1.494 | - | 1.499 | - | 1.515 | - | 1.504 | 1.509 | - |

Symmetry code for (1): $(a)-x, 1-y,-z$; for (2): $(a)-x, y, 2-z . \quad \dagger$ Regression equation used for $\mathrm{C}-\mathrm{N}$ bonds is $d=1.444-0.184 p_{\mathrm{P}}$ and for $\mathrm{C}-\mathrm{C}$ bonds $d=1.458-0.143 p_{\mathrm{P}}$ For single bonds $\mathrm{C} 2-\mathrm{C} 21$ and $\mathrm{C} 5-\mathrm{C} 53$ the Pauling equation is used (Pauling, 1980 ): $d=1.504-0.3128 p_{\mathrm{P}} /$ $\left(0.84 p_{\mathrm{P}}+1\right) . \quad \ddagger$ Regression equation used for $\mathrm{C}-\mathrm{N}$ bonds is $d=1.454-0.178 p_{\mathrm{VESCF}}$ and for $\mathrm{C}-\mathrm{C}$ bonds $d=1.509-0.185 p_{\mathrm{VESCF}}$

However, there are discrepancies for structure (2) (Table 5) involving the bonds next to the disordered atoms N4 and C4. The experimental value of the C4C51 bond length [ $1.375(13) \AA$ A $]$ is shorter whereas the $\mathrm{C} 51-\mathrm{N} 4$ bond $[1.434(10) \AA$ ] is longer than the theoretically derived values.
3.2. Crystal packing and $\pi \cdots \pi$ interactions of the diazapyrenes and pyrene-like molecules
3.2.1. Classification of the crystal packings of condensed polycyclic aromatic hydrocarbons. In the search for correlations between the molecular structure and molecular packing in crystals some parameters of geometrical and electronic structures may be defined; molecular properties are related to these parameters, while many crystal properties are the consequence of crystal-packing characteristics and intermolecular interactions. Organic compounds rich in $\pi$ aromatic systems develop certain types of crystal packings, first classified by Robertson (1951). Since then, a large collection of valuable and accurate crystal structure data has been stored in the CSD, and more precise classifications based on accurate data have become possible.

Gavezzotti and Desiraju (Gavezzotti \& Desiraju, 1988; Desiraju \& Gavezzotti, 1989) have recognized four characteristic crystal-packing patterns of planar condensed polycyclic aromatic hydrocarbons: herringbone (HB), sandwich-herringbone (SH), $\beta$ type and $\gamma$ type (Figs. $8 a-c$ ). The main distinguishing factor among the motifs is the relative orientation of the molecular planes in the crystal, which influences the length of the shortest cell axis $p$ (Fig. 3). The HB type is characterized by the closest molecules oriented in a nonparallel
fashion and the shortest axis in the range 5.4-8.0 $\AA$. In the sandwich-herringbone motif (Fig. 8a) there are sandwich-like pairs organized in herringbone fashion with the shortest axis longer than $8 \AA$. The $\beta$ type (Fig. $8 b$ ) is characterized by a short axis of about $4 \AA$ with the stacked molecules resembling graphite layers (which are separated by about $3.35 \AA$; Wells, 1975). One of the two closest layers is translated and its shift is defined by the centre-to-centre offset vector (Fig. 3). In graphite, its value is $1.42 \AA$, being close to the $\mathrm{C}-\mathrm{C}$ bond in benzene, 1.394 (7) A. Goddard et al. (1995) introduced the centre-to-centre offset vector for detecting $\pi \cdots \pi$ interactions. In general, the shortest values of the offset parameter are typical of the $\beta$ motif (e.g. $1.48 \AA$ in tetrabenzoheptacene; Goddard et al., 1995). The offset parameter values plausibly reveal the highest degree of $\pi \cdots \pi$ interactions in the $\beta$ pattern. The $\gamma$ type (Fig. $8 c$ ) comprises parallel-displaced molecules with the shortest axis in the range $4.6-5.4 \AA$. According to the analysis of 32 structures of polycyclic aromatic hydrocarbons given by Desiraju \& Gavezzotti (1989) the essential parameter for the crystal-packing classification is the shortest cell axis always being a screw-axis direction in monoclinic or orthorhombic space groups. Kitaigorodsky (1973) found that preferred space groups are those which allow close packing with molecules of $C_{i}$ symmetry such as $P \overline{1}, P 2_{1} / c$ (or equivalents), $C 2 / c$ or orthorhombic $P b c a$. Goddard et al. (1995) detected only two space groups, $P 2_{1} / c$ (or equivalents) and $C 2 / c$ for the planar polycyclic aromatic hydrocarbons.
3.2.2. Crystal packing of (1), (2) and pyrene analogues. The molecular overlap in crystals of (1) and (2) is shown in Figs. $9(a)$ and $9(b)$, respectively. The crystal packings of the $\beta$ type are shown for (1) and (2) in Figs. 10(a) and
$10(b)$, respectively. The essential parameters for the classification of the packing type of the molecules in Fig. 2 are listed in Table 6. Two categories of parameters are used. Geometrical parameters are defined in Fig. 3: $\varphi, \theta$ and $d$ are the parameters taken from Goddard et al. (1995) whereas stacking areas and interactive volume are defined in this work. The elements of electronic structure used in the analysis are mentioned in $\S 1$.

In the 'sample' subjected to analysis, the space group $P 2_{1} / c$ (or $P 2_{1} / a$ and $\left.P 2_{1} / n\right)$ prevails $(\sim 85 \%)$ with high domination of the $\beta$ motif, including the diazapyrenes (1) and (2). The classification according to the shortest axis (parallel to the monoclinic twofold axis) is strictly valid for the class of pyrene and its analogues. For packings of the $\beta$ type the shortest axis value is on average $0.4 \AA$ longer than the sum of the van der Waals radii. Stacking typical of pyrene and analogous systems also occurs between conjugated systems (Fig. 2, Table 6) such as 1,6-dioxopyrene (VOXLOJ), ellagic acid (ELLAGC), naphtho[1,8-c, $\left.d: 4,5-c^{\prime}, d^{\prime}\right]$ bis[1,2,6]selenadiazine (NAPSEZ10) and its sulfur analogue (NAPTDZ10). Among the structures studied, two cases of quasi- $\beta$ type were detected: the structure of decachloropyrene ( $\beta^{*}$ ) (DECPYR10) and $N$-tetrachloro-salicylidene-1-pyrenylamine stacked by salicylidene moiety $\left(\beta^{* *}\right)$ (TAHBUZ). An influence of the additional conjugated system to the aromatic one on the crystal-packing motif can be recognized in the crystal structures of nitrobenzene derivatives; their crystalpacking motif is classified as the pseudo-herringbone pattern (André et al., 1997a,b). The molecule of decachloropyrene was selected as a single example of a nonplanar system also stacked with an average separation distance of 3.715 (3) $\AA$, whereas in TAHBUZ the separation is 3.673 (8) $\AA$. The common characteristic of the pyrene analogues with $\beta$-type stacking is the tilt angle $\varphi$ (Fig. 3) of $60 \pm 4^{\circ}$. Owing to the diads in the sandwich-herringbone pattern, this angle is small ( $\simeq 16^{\circ}$, Fig. $8 a$ ). However, in this packing the centres of the molecules are on a line which does not coincide with the
crystallographic axis; an angle of about $60^{\circ}$ between this line and the normal to the plane of the aromatic ring characterizes the sandwich-herringbone pattern. In the $\gamma$ type (Fig. 8c) $\varphi \simeq 45^{\circ}$. The $\beta$ type is also characterized by a short offset vector $v$ (Fig. 3, Table 6). In many cases, the offset vector is collinear with the molecular elongation axis. Diagonal sliding can be influenced by the presence of polar ring heteroatom(s) (Table 6, O in VOXLOJ, S in DOXTEP), small substituents as in 2,6dimethylpyrene (Fig. 2, DMPYRN) and steric hindrance as in the crystal packing of 1,3,6-tetrafluoro-2,4,5,7,9,10hexachloropyrene and decadeuteropyrene (Fig. 2, Table


Fig. 9. Molecular overlap in crystals of (a) (1) and (b) (2).


Fig. 8. Crystal-packing types: (a) sandwich-herringbone (SH) motif of decadeuteropyrene (Knight et al., 1996); (b) $\beta$ type, naphtho[1,8-c,d:4,5$\left.c^{\prime} d^{\prime}\right]$ bis $[1,2,6]$ selenadiazine (Gieren et al., 1980); (c) $\gamma$ type, 1,3,6,8-tetrafluoro-2,4,5,7,9,10-hexachloropyrene (Hazell \& Weigelt, 1975) (F and Cl atoms omitted for clarity).

## Table 6. Parameters relevant for definition and classification of crystal-packing types for pyrenes and analogues

Packing types are sandwich-herringbone (SH), $\beta, \gamma$ and quasi $-\beta$ types ( $\beta^{*}, \beta^{* *}$ ). $p$ is the shortest crystallographic axis, $d$ is the interplanar distance between parallel neighbouring rings and $v$ is the corresponding centre-to-centre offset ( $\AA$ ). $\varphi$ is the angle between the $p$ axis and the ring plane and $\theta$ is the interplanar angle betwen the adjacent stacks ( ${ }^{\circ}$ ). $S_{1}, S_{2}$ and $S_{3}$ are stacking areas ( $\AA^{2}$ ). $V$ is the interactive volume $\left(\AA^{3}\right) . E$ is the average atomic electronegativity after Pauling. $N$ is the number of delocalized, localized and free pair electrons. $Q$ is the sum of the partial atomic charges of the pyrene skeleton ( 16 non-H atoms) calculated using MOPAC-PM3.

|  | Space group | $Z$ | Packing type | $p$ | $\varphi$ | $d$ | $\theta$ | $v$ | $S_{1}$ | $S_{2}$ | $S_{3}$ | V | E | $N$ | $Q$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PYRENE02 | $P 2_{1} / a$ | 4 | SH | 8.470 (10) | 16.41 (3) | 3.528 (3) | 83.37 (4) | 1.762 | 12.1 | 12.1 | 0 | 42.5 | 2.38 | 16 | -1.047 |
| pyrene $\dagger$ | $P 2_{1} / a$ | 4 | SH | 8.22064 (1) | 16.16 (15) | 3.433 (6) | 76.71 (7) | 1.443 | 14.2 | 14.2 | 0 | 48.6 | 2.38 | 16 | -1.047 |
| VOXLOJ | $P 2_{1} / n$ | 2 | $\beta$ | 3.922 (1) | 62.02 (13) | 3.462 (12) | 55.95 (19) | 1.840 | 10.2 | 17.6 | 2.6 | 70.3 | 2.48 | 22 | -0.956 |
| DOXTEP | $P 2_{1} / n$ | 2 | $\beta$ | 4.026 | 60.06 | 3.489 | 59.88 | 2.009 | 10.4 | 19.6 | 1.8 | 72.8 | 2.41 | 22 | -0.963 |
| NAPTDZ10 | $P 21 / a$ | 2 | $\beta$ | 3.794 (4) | 63.79 (7) | 3.404 (2) | 51.3 (1) | 1.676 | 13.4 | 18.8 | 3.0 | 91.4 | 2.55 | 30 | -0.525 |
| NAPSEZ10 | $P 2_{1} / a$ | 2 | $\beta$ | 3.863 (5) | 62.32 (7) | 3.420 (15) | 49.32 (10) | 1.782 | 13.8 | 19.5 | 3.7 | 91.8 | 2.54 | 30 | -0.529 |
| (1) | $P 2{ }_{1} / c$ | 2 | $\beta$ | 4.0246 (5) | 58.80 (5) | 3.442 (18) | 10.8 (2) | 2.085 | 10.6 | 16.3 | 4.4 | 70.6 | 2.41 | 20 | -0.864 |
| (2) $\ddagger$ | C2/m | 2 | $\beta$ | 3.9615 (5) | 64.34 (12) | 3.571 (2) | 0 | 1.715 |  |  |  |  | 2.41 | 20 | -0.740 |
| DMPYRN§ | $P 2{ }_{1} / c$ | 4 | SH | 8.1554 (5) |  | 3.45 |  | 1.909 | 8.8 | 8.8 | 0 | 30.5 | 2.37 | 16 | -0.994 |
| ELLAGC | $P 2{ }_{1} / c$ | 2 | $\beta$ | 3.745 | 64.18 (5) | 3.370 (6) | 8.88 (7) | 1.631 | 10.0 | 16.9 | 4.2 | 67.3 | 2.69 | 48 | 0.371 |
| KENDEM | $P 2{ }_{1} / c$ | 2 | $\gamma$ | 5.305 (1) | 41.16 (3) | 3.491 (2) | 82.32 (5) | 3.994 | 6.2 | 12.5 | 0 | 21.8 | 2.68 | 42 | 0.627 |
| DAHNEF | $P 2{ }_{1} / c$ | 4 | $\beta$ | 3.877 (1) | 63.93 (5) | 3.484 (6) | 52.13 (7) | 1.704 | 11.8 | 16.9 | 2.1 | 82.4 | 2.41 | 16 | -0.960 |
| TFHCPY10 | $P 2_{1} / a$ | 2 | $\gamma$ | 4.864 (5) | 45.18 (5) | 3.450 (2) | 89.64 (7) | 3.429 | 4.4 | 8.5 | 0 | 15.3 | 2.89 | 76 | -0.610 |
| DECPYR10^ | $P 2_{1} / n$ | 4 | $\beta^{*}$ | 7.494 (5) | 82.46 (4) | 3.715 (3) | 15.08 (6) | 2.8 | 5.4 | 7.0 | 3.8 | 19.9 | 2.77 | 76 | -1.286 |
| BUTPYR10† $\dagger$ | $P \overline{1}$ | 1 | - | 6.138 (5) | 32.42 (3) | 3.292 (2) | 0 | 5.181 | 0 | 0 | 0 | 0 | 2.34 | 16 | -1.001 |
| VAMZIS | $P 2_{1} / a$ | 4 | $\gamma$ | 5.018 (6) | 43.03 (15) | 3.424 (8) | 86.1 (2) | 3.668 | 1.7 | 3.4 | 0 | 5.9 | 2.42 | 16 | -1.016 |
| TAHBUZ ${ }_{\text {\% }}$ | $P 2_{1} / a$ | 4 | $\beta^{* *}$ | 8.197 (2) | 56.53 (6) | 3.673 (8) | 57.21 (9) | 10.112 |  |  |  |  | 2.52 | 18 | -0.956 |
| ZEDDIV | Pa | 2 | $\gamma$ | 4.815 (1) | 45.57 (3) | 3.438 (6) | 88.85 (8) | 3.371 | 4.1 | 8.2 | 0 | 14.1 | 2.42 | 18 | -0.968 |
| KASZAF01 | $P 2_{1} / a$ | 2 | $\beta$ | 3.795 (1) | 63.33 (3) | 3.390 (6) | 34.52 (5) | 1.269 | 15.3 | 20.3 | 10.4 | 103.9 | 2.44 | 20 | -0.903 |

$\dagger$ Deuteropyrene (Knight et al., 1996). $\ddagger$ Stacking areas are not calculated because of the disorder. § Missing coordinates (Ingartinger et al., 1977, an entry from the CSD). © Average values of $v$ and $S_{1} . \quad \dagger$ Non-aromatic packing type. $\quad \forall$ Stacking areas are not calculated since the pyrene rings are not stacked with each other but with another aromatic system (salicylidene).


Fig. 10. Crystal packing of the $\beta$ type in (a) (1) and (b) (2).
6, TFHCPY10). In the structure of (1), the presence of endocyclic nitrogen produces a small diagonal shift. The values of the offset parameter for (1) and (2) are 2.085 and $1.715 \AA$, respectively. The smaller value of this parameter in the structure of (2) can be explained by the disorder, which changes the orientation of the vector along the $\mathrm{C} 4-\mathrm{N} 4$ bond from one stacked molecule to the other. The short $v$ vector denotes dominating $\pi \cdots \pi$ interaction which characterizes $\beta$ and SH types. The extremely short offset parameter of $1.269 \AA$ in $N, N^{\prime}$ -disalicylidene-1,6-pyrenediamine (Table 6, KASZAF01, Fig. 2) is due to the stacks of pyrene and attached aromatic substituents. For the $\gamma$ type a larger offset occurs $(3.37<v<3.99 \AA)$. The common characteristic for SH and $\gamma$ types (Figs. $8 a$ and $8 c$, Table 6) is an almost perpendicular orientation of the adjacent stacks $(\theta>$ $80^{\circ}$ ). The interactive volume and the overlapping surfaces (defined in Fig. 3) also illustrate the degree of $\pi \cdots \pi$ interaction. The interactive volume is largest for the $\beta$ type $\left(67.3<V<103.9 \AA^{3}\right)$, smaller for $\mathrm{SH}(30.5<$ $V<48.6 \AA^{3}$ ), and smallest for the $\gamma$ type ( $V<21.8 \AA^{3}$ ). The overlapping surfaces (Fig. 3) are very distinctive for a certain packing pattern. In the SH type with two molecules in a pair, $S_{1}=S_{2}$ whereas $S_{3}=0$. In the $\beta$ type with a high degree of $\pi \cdots \pi$ interaction, the overlapping surfaces between two molecules are large, particularly $S_{2}$, whereas the overlapping surfaces among the three closest neighbours $S_{3}$ are smaller than $S_{1}+S_{2}$. For the $\gamma$ type $S_{2}>S_{1}$ and $S_{3}=0$ (Fig. 3, Fig. 8c). The geometrical parameters are sufficient to discriminate unambiguously among patterns as illustrated by Fig. 11.

However, from the correlations between the molecular characteristics, including the elements of electronic structure and crystal packing, additional information for


Fig. 11. Scatterplots used to discriminate specific packing types of pyrenes and analogues. (a) The shortest axis versus $\theta$. (b) The shortest axis versus $V$.
classification of the packing patterns of these aromatics can be gained. Over forty relationships between the geometrical and the electronic structure parameters, based on second-order polynomial regression analysis, were examined and only those with correlation coefficients $r \geq 0.85$ were used: $V$ versus $N$ (Fig. 12a), V versus $E$ (Fig. $12 b$ ) and $S_{2}$ versus $N$ (Fig. 12c), $S_{2}$ versus $E$ (Fig. $12 d$ ) reveal the optimal ranges of the electronic structure parameters for a certain packing pattern, being more restrictive for $\beta$ than for $\gamma$ types (Table 6). Moreover, a very narrow range of $N$ and $E$ can satisfy the SH packing arrangement.

Correlations of geometrical parameters $S_{1}, S_{2}, V, v$ and $Q$ (Table 6, Figs. 13a-d) are shown. Comparison of both $S_{1}$ and $S_{2}$ versus $Q$ shows a similar trend; the molecules to be stacked are limited by the values of their partial charges. In general, for $\beta$ and even more for SH types with a high degree of $\pi$ interactions, only narrow ranges of $N, E$ and $Q$ are tolerated. On the contrary, in the $\gamma$ type there is no such close contact between neighbouring molecules which can be disturbed by repulsions and thus $N, E$ and $Q$ are distributed over a wide range.


Calculations of the potential energy between the relevant molecule and its neighbours at a maximum distance of $15 \AA$ in the unit cell obtained using PLUTO (Motherwell, 1997) revealed that the lowest energies were obtained for stacked pairs in $\beta$ and SH arrangements. However, this type of calculation should be treated with caution, since the parameterization should take care of intra- and intermolecular interactions, the contribution from which should be weighted individually for each type of molecule. For this reason, calculations were carried out only for crystals free from hydrogen bonds and polar groups. The calculations performed for diazapyrenes (1) and (2), both of $\beta$ type, detected the lowest energy for the two closest molecules. Disorder in (2) changes the orientation of the $\mathrm{C} 4 a-\mathrm{N} 4$ vector; instead of a small repulsion, attraction between stacked molecules occurs. For this reason, the offset parameter is smaller for (2) than for (1) (Table 6). The structure of (2) can be described by an infinite sequence of energetically well balanced $A B$ layers. These results are in agreement with those obtained from ab initio calculations for a benzene dimer (Hobza et al., 1994) which found the parallel-displaced structure to be

(b)

(d)

Fig. 12. Correlations of geometrical parameters $V$ and $S_{2}$ (definitions given in Fig. 3) and electronic structures using parameters $N$ and $E$ (defined in Table 6) used to resolve the packing patterns. A second-order polynomial regression was used.
slightly more stable than the displaced T-shaped structures. The empirical rules of Hunter \& Sanders (1990) are in favour of the T-shaped molecules. Recent calculations performed by Chipot et al. (1996) on benzene and toluene dimers in the gas phase and in an aqueous medium have not resolved the problem of orientational preference in general. However, these authors stress the importance of taking into account not only the electrostatic and dispersion interactions between the aromatic moieties but possible steric hindrance, particularly in analysing $\pi \cdots \pi$ interactions in proteins. Steric hindrance caused by the bulky tert-butyl groups disables stacking in the crystal structure of 2,7-di-tert-butylpyrene (BUTPYR10, Fig. 2, Table 6). This evidence also supports the observations of Chipot et al. (1996).

In order to learn more about the $\pi \cdots \pi$ interactions of pyrene and analogues, a search for molecular complexes with other aromatic molecules was performed using the CSD. Of about 40 complexes detected, only those of the highest accuracy ( $R \leq 0.07$ ) were selected according to the criteria described in $\S 2.4$. The examination of their structures reveals stacking of pyrene and aromatic molecules in an $A B$ sequence with $d \simeq 3.50 \AA$ (where $d$
is the distance between the centres of mass). Formation of such molecular complexes can be considered as interaction between $\pi$-donor HOMOs and $\pi$-acceptor LUMOs of molecules in alternating layers in the unit cell (Bleidelis et al., 1976; Purcell \& Kotz, 1977), which can be treated as charge-transfer complexes (Zacharias et al., 1991). Some of these molecular adducts are of interest as DNA intercalators. The charged diazaprenium species can be as good intercalators as ethidium (Steiner-Biočić et al., 1996; Sarfati et al., 1995; MeyerAlmes \& Porschke, 1993). On the other hand, stable adducts with layered structures can be anisotropic conductors of electricity; current flows easily normal to the molecular planes but negligibly in directions parallel to the aromatic planes (one-dimensional organic 'metals').

## 4. Conclusions

Classification of the crystal packing of aromatic hydrocarbons derived by Gavezzotti \& Desiraju (1988) and Desiraju \& Gavezzotti (1989) using geometrical parameters is applicable to the pyrenes, diazapyrenes and


Fig. 13. Correlations of geometrical parameters (defined in Fig. 3) $S_{1}, S_{2}, V, v$ and $Q$ (definitions in Table 6). A second-order polynomial regression was used.
analogous conjugated systems. Correlations of geometrical and electronic structure parameters relate properties of molecular and crystal structures:
(i) plots of interactive volume $V$ versus average electronegativity $E$, and overlapping surface $S_{2}$ versus $E$, reveal that for maximum values of $V$ and $S_{2}$ the average electronegativity is about 2.5 and characterizes the $\beta$ packing type ( $E$ for graphite is 2.5 );
(ii) plots of overlapping surfaces and interactive volume versus the sum of partial atomic charges, $Q$, show that $Q \simeq 0$ when $V$ and $S_{2}$ are at a maximum (for graphite, $Q=0$ ).

From these correlations, a comparison between graphite and $\beta$-type packing is possible. Thus, the $\beta$ type can be described as the packing motif with a high degree of $\pi \cdots \pi$ interactions. Most of the compounds analysed reveal crystal packing of the $\beta$ type characterized by stacked displaced layers with a high contribution of $\pi \cdots \pi$ interactions. The high predominance of the single space group $\left(P 2_{1} / c\right)$ detected in the crystal packing with defined parameters of the classification of the packing patterns make these molecules good candidates for crystal structure prediction. However, the main obstacle still remains of the feasible energetic evaluation of the proposed model (van Eijck \& Kroon, 1997).

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